

MATHEMATICS

101. In a town of 10,000 families it was found that 40% families buy newspaper A, 20% families buy newspaper B and 10% families buy newspaper C, 5% families buy A and B, 3% buy B and C and 4% buy A and C. If 2% families buy all the three newspaper, then number of families which buy A only is

- a) 3100 **b) 3300**
c) 2900 d) 1400

102. if $F(x) = \left(f\left(\frac{x}{2}\right)\right)^2 + \left(g\left(\frac{x}{2}\right)\right)^2$ where $f''(x) = -f(x)$ and $g(x) = f'(x)$ and given that $F(5) = 5$, then $F(10)$ is equal to

- a) 5** b) 10
c) 0 d) 15

103. Let $f(x+y) = f(x) f(y)$ for all x and y . Suppose $f(5) = 2$ and $f'(0) = 3$. Find $f'(5)$.

- a) 3 **b) 6**
c) 9 d) 0.6

104. If $|z| = 1$ and $\omega = \frac{z-1}{z+1}$ (where $z \neq -1$), then $\text{Re}(\omega)$ is

- a) 0** b) $\frac{1}{|z+1|^2}$
c) $\left|\frac{z}{z+1}\right| \cdot \frac{1}{|z+1|^2}$ d) $\frac{\sqrt{2}}{|z+1|^2}$

105. Let z_1 and z_2 be two roots of the equation $z^2 + az + b = 0$, z being complex. Further, assume that the origin, z_1 and z_2 form an equilateral triangle, then

- a) $a^2 = b$ b) $a^2 = 2b$
c) $a^2 = 3b$ d) $a^2 = 4b$

106. For all complex numbers z_1, z_2 satisfying $|z_1| = 12$ and $|z_2 - 3 - 4i| = 5$, the minimum value of $|z_1 - z_2|$ is

- a) 0 **b) 2**
c) 7 d) 17

107. Let λ and α be real, Find the set of all values of λ for which the system of linear equations

$$\lambda x + (\sin \alpha) y + (\cos \alpha) z = 0$$

$$x + (\cos \alpha) y + (\sin \alpha) z = 0$$

$$-x + (\sin \alpha) y - (\cos \alpha) z = 0$$

has a nontrivial solution. For $\lambda = 1$, find the value of α .

- a) $n\pi \pm \pi/8 + \pi/8$** b) $n\pi \pm \pi/4 + \pi/4$
c) $\pm n\pi + \pi/4 + \pi/4$ d) $\pm n\pi + \pi/4 + \pi/8$

108. If p and q are the roots of $x^2 + px + q = 0$, then

- a) $p = 1, q = -2$** b) $p = -2, q = 1$
c) $p = 1, q = 0$ d) $p = -2, q = 0$

109. If $a_1, a_2, \dots, a_n, \dots$ are in GP then the determinant

$$\Delta = \begin{vmatrix} \log a_n & \log a_{n+1} & \log a_{n+2} \\ \log a_{n+3} & \log a_{n+4} & \log a_{n+5} \\ \log a_{n+6} & \log a_{n+7} & \log a_{n+8} \end{vmatrix}$$

is equal to

- a) 2 b) 4
c) 0 d) 1

110. Let $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$ and $(10)B = \begin{bmatrix} 4 & 2 & 2 \\ -5 & 0 & \alpha \\ 1 & -2 & 3 \end{bmatrix}$. If B is

the inverse of matrix A, then α

- a) -2 b) 1
c) 2 **d) 5**

111. If the system of equations $x+ay=0$, $az+y=0$ and $ax+z=0$ has infinite solution, then values of a is
a) -1 b) 1
c) 0 d) no real value

112. Let M and N be two even order non-singular skew-symmetric matrices such that $MN=NM$. If P^T denotes the transpose of P , then $M^2 N^2 (M^T N)^{-1} (MN^{-1})^T$ is equal to
a) M^2 b) $-N^2$
c) $-M^2$ d) MN

113. The value of the determination $\begin{vmatrix} 1 & a & a^2-bc \\ 1 & b & b^2-ac \\ 1 & c & c^2-ab \end{vmatrix}$ is.....
a) 1 b) 3
c) 100 **d)** 0

114. Numbers greater than 1000 but not greater than 4000 which can be formed with the digits 0, 1, 2, 3, 4 (repetition of digits is allowed), are
a) 350 **b)** 375
c) 450 d) 576

115. How many words can be formed with the letters of the words MATHEMATICS by rearranging them
a) $\frac{11!}{2! 2!}$ b) $\frac{11!}{2!}$
c) $\frac{11!}{2! 2! 2!}$ d) $11!$

116. In how many ways can 6 persons be selected from 4 officers and 8 constables, if at least one officer is to be included
a) 224 b) 672
c) 896 d) none of these

117. The product of n positive numbers is unity. Then their sum is
a) a positive integer b) divisible by n
c) equal to $n+1/n$ **d)** never less than n .

118. If x is positive, the first negative term in the expansion of $(1+x)^{27/5}$ is
a) 7th term b) 5th term
c) 8th term d) 6th term

119. Let x be the arithmetic mean and y, z be the two geometric means between any two positive numbers. Then $\frac{y^3 + z^3}{xyz} =$
a) 4 b) 0.2
c) 2 d) 20

120. Sum of the infinite series $1+2+\frac{1}{2!}+\frac{2}{3!}+\frac{1}{4!}+\frac{2}{5!}+\dots$ is
a) e^2 b) $e + e^{-1}$
c) $\frac{e - e^{-1}}{2}$ **d)** $\frac{3e - e^{-1}}{2}$

121. The interior angles of a polygon are in A.P. the smallest angle is 120° and the common difference is 5° . Find the number of sides of the polygon.
a) 16 b) 9
c) 4 d) 12

122. If the sum of first n terms of an A.P. is cn^2 , then the sum of squares of these n terms is
a) $\frac{n(4n^2-1)c^2}{6}$ b) $\frac{n(4n^2+1)c^2}{3}$
c) $\frac{n(4n^2-1)c^2}{3}$ **d)** $\frac{n(4n^2+1)c^2}{6}$

123. The domain of $f(x) = \frac{\log_2(x+3)}{x^2+3x+2}$ is

- a) $\mathbb{R} - \{-1, -2\}$ b) $(-2, +\infty)$
c) $\mathbb{R} - \{-1, -2, -3\}$ **d) $(-3, +\infty) - \{-1, -2\}$**

124. Let $g(x) = 1 + x - [x]$ and $f(x) = \begin{cases} -1, & x < 0 \\ 0, & x = 0 \\ 1, & x > 0 \end{cases}$, then for all

$x, f(g(x))$ is equal to

- a) x **b) 1**
c) $f(x)$ d) $g(x)$

125. For $x > 0$, $\lim_{x \rightarrow 0} [(\sin x)^{1/x} + (1/x)^{\sin x}]$ is

- a) 0 b) -1
c) 1 d) 2

126. $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\int_0^{\sec^2 x} f(t) dt}{x^2 - \frac{\pi^2}{16}}$ equals

- a) $\frac{8}{\pi} f(2)$** b) $\frac{2}{\pi} f(2)$
c) $\frac{2}{\pi} f(1/2)$ d) $4f(2)$.

127. If $f(x) = \frac{e^x}{1+e^x}$, $I_1 = \int_{f(-a)}^{f(a)} x g\{x(1-x)\} dx$, and

$I_2 = \int_{f(-a)}^{f(a)} g\{x(1-x)\} dx$, then value of I_2/I_1 is

- a) 2 b) -3
c) -1 **d) 1**

128. Let $f(x)$ be a function satisfying $f'(x) = f(x)$ with $f(0) = 1$ and $g(x)$ be a function that satisfies $f(x) + g(x) = x^2$. Then the value of the integral $\int_0^1 f(x) g(x) dx = x^2$. Then the value of the integral $\int_0^1 f(x) g(x) dx$, is

- a) $e - \frac{e^2}{2} - \frac{5}{2}$ b) $e + \frac{e^2}{2} - \frac{3}{2}$
c) $e - \frac{e^2}{2} - \frac{3}{2}$ d) $e + \frac{e^2}{2} + \frac{5}{2}$

129. The value of $\int_0^{\pi/2} \frac{dx}{1+\tan^3 x}$ is

- a) 0 b) 1
c) $\pi/2$ **d) $\pi/4$**

130. If $\int_0^x f(t) dt = x + \int_x^1 t f(t) dt$ then the value of $f(1)$ is

- a) 1/2** b) 0
c) 1 d) -1/2

131. The value of $\int_{-2}^2 |1-x^2| dx$ is.....

- a) 8 b) 14
c) 4 d) 40

132. The general solution of the equation $(e^y + 1) \cos x dx + e^y \sin x dy = 0$ is

- a) $(e^y + 1) \cos x = c$ b) $(e^y - 1) \sin x = c$
c) $(e^y + 1) \sin x = c$ d) None of these

133. If $x dy = y(dx + y dy)$, $y > 0$ and $y(1) = 1$, then $y(-3)$ is equal to

- a) 1 **b) 3**
c) 5 d) -1

134. The integration factor of the differential equation

$$\frac{dy}{dx} + \frac{1}{x} y = 3x \text{ is}$$

- a) x b) $\ln x$
c) 0 d) ∞

135. The solution of the differential equation

$$x \frac{dy}{dx} = y(\log y - \log x + 1) \text{ is}$$

- a) $y = xe^{cx}$ b) $y + xe^{cx} = 0$
c) $y + e^x = 0$ d) None of these

136. The eccentricity of an ellipse with its centre at the origin, is $1/2$ if one of the directrices is $x = 4$, then the equation of the ellipse is

- a) $3x^2 + 4y^2 = 1$ b) $3x^2 + 4y^2 = 12$
c) $4x^2 + 3y^2 = 12$ d) $4x^2 + 3y^2 = 1$

137. The greatest distance of the point $P(10, 7)$ from the circle $x^2 + y^2 - 4x - 2y - 20 = 0$ is

- a) 10 unit b) 15 unit
c) 5 unit d) None of these

138. The parabolas $y^2 = 4x$ and $x^2 = 4y$ divide the square region bounded by the lines $x = 4$, $y = 4$ and the coordinate axes. If s_1 , s_2 , s_3 are respectively the areas of these parts numbered from top to bottom, then $s_1 : s_2 : s_3$ is

- a) $1 : 1 : 1$ b) $2 : 1 : 2$
c) $1 : 2 : 3$ d) $1 : 2 : 1$

139. The area of the triangle formed by the line $4x^2 - 9xy - 9y^2 = 0$ and $x = 2$ is

- a) 2 b) 3
c) $10/3$ d) $20/3$

140. The value of k so that $x^2 + y^2 + kx + 4y + 2 = 0$ and $2(x^2 + y^2) - 4x - 3y + k = 0$ cut orthogonally is

- a) $\frac{10}{3}$ b) $\frac{-8}{3}$
c) $\frac{-10}{3}$ d) $\frac{8}{3}$

141. The equation to the circle with origin as center passing through the vertices of an equilateral triangle whose median is of length $3a$ is

- a) $x^2 + y^2 = 9a^2$ b) $x^2 + y^2 = 16a^2$
c) $x^2 + y^2 = a^2$ d) None of these

142. A square is inscribed in the circle $x^2 + y^2 - 2x + 4y - 93 = 0$ with its sides parallel to the coordinate axes. The coordinates of its vertices are

- a) $(-6, -9), (-6, 5), (8, -9)$ and $(8, 5)$
b) $(-6, 9), (-6, -5), (8, -9)$, and $(8, 5)$
c) $(-6, -9), (-6, 5), (8, 9)$, and $(8, 5)$
d) $(-6, -9), (-6, 5), (8, -9)$, and $(8, -5)$

143. The points $A(5, -1, 1)$; $B(7, -4, 7)$; $C(1, -6, 10)$ and $D(-1, -3, 4)$ are vertices of a

- a) Square b) Rhombus
c) Rectangle d) None of these

144. Find the equation of the plane passing through $(2, 1, 0)$, $(4, 1, 1)$, $(5, 0, 1)$. Find the point Q such that its distance from the plane is equal to the distance of point $P(2, 1, 6)$ from the plane and the line joining P and Q is perpendicular to the plane.

- a) $9/2$ cubic unit b) $9/4$ cubic unit
c) 4 cubic unit d) $2/9$ cubic unit

145. The points D,E,F divide BC, CA and AB of the triangle ABC in the ratio 1 : 4, 3 : 2 and 3 : 7 respectively and the point K divides AB in the ratio 1:3, then $(\vec{AD} + \vec{BE} + \vec{CF}) : \vec{CK}$ is equal to

- a) 1 : 1 **b) 2 : 5**
 c) 5 : 2 d) None of these

146. If a, b, c are non-coplanar unit vectors such

that $a \times (b \times c) = \frac{b+c}{\sqrt{2}}$, then the angle between a and b is

- a) $\pi/4$ b) $\pi/2$
c) $3\pi/4$ d) π

147. Three numbers are chosen at random without replacement from $\{1, 2, \dots, 10\}$. The probability that the minimum of the chosen numbers is 3, or their maximum is 7, is

- a) 13/60 b) 13/30
 c) 60/13 d) 60/3

148. Out of $3n$ consecutive natural numbers, 3 natural numbers are chosen at random without replacement. The probability that the sum of the chosen numbers is divisible by 3 is

- a) $\frac{n(3n^2 - 3n + 2)}{2}$ b) $\frac{(3n^2 - 3n + 2)}{2(3n-1)(3n-2)}$
c) $\frac{(3n^2 - 3n + 2)}{(3n-1)(3n-2)}$ d) $\frac{n(3n-1)(3n-2)}{3(n-1)}$

149. one bag contains 5 white and 4 black balls. Another bag contains 7 white and 9 black balls. A ball is transferred from the first bag to the second and then a ball is drawn from second. The probability that the ball is white, is

- a) 8/17 b) 40/153
 c) 5/9 **d) 4/9**

150. If $\alpha + \beta = \pi/2$ and $\beta + \gamma = \alpha$, then $\tan \alpha$ equals

- a) $2(\tan \beta + \tan \gamma)$ b) $\tan \beta + \tan \gamma$
c) $\tan \beta + 2\tan \gamma$ d) $2\tan \beta + \tan \gamma$